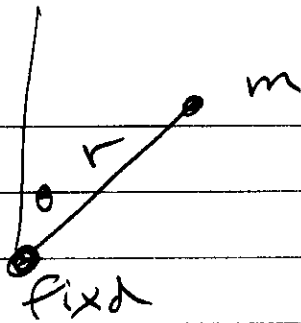


3)



use polar coordinates  
 $U = mgr \cos \theta$

$$T = \frac{1}{2} m r^2 \dot{\theta}^2 + \frac{1}{2} m r^2 \sin^2 \theta \dot{\varphi}^2$$

constraint:  $r = \text{constant}$

$$L = T - U = \frac{1}{2} m r^2 \dot{\theta}^2 + \frac{1}{2} m r^2 \sin^2 \theta \dot{\varphi}^2 - mgr \cos \theta + \lambda (r - c)$$

$$\theta: \frac{d}{dt} m r^2 \dot{\theta} - m r^2 \sin \theta \cos \theta \dot{\varphi}^2 - mgr \sin \theta = 0$$

$$\varphi: \frac{d}{dt} (m r^2 \sin^2 \theta \dot{\varphi}) = 0$$

$$r: m r \dot{\theta}^2 + m r \sin^2 \theta \dot{\varphi}^2 - mgr \cos \theta + \lambda = 0$$

$$4) T = \sum_k F_k(q_k) \dot{q}_k^2 \quad V = \sum_k V_k(q_k)$$

$$EL: \frac{d}{dt} (F_k(q_k) \dot{q}_k) - F'_k \dot{q}_k^2 + V'(q_k) = 0$$

each equation only depends on  $q_k$   
 $\Rightarrow$  problem is separable.