

$$\Rightarrow q = (e^Q - 1)^2 - \frac{p^2}{4e^{2Q}}$$

$$\Rightarrow \left. \frac{\partial q}{\partial Q} \right|_{p \text{ fixed}} = 2(e^Q - 1)e^Q + \frac{p^2 \cdot 2e^{2Q}}{4e^{4Q}}$$

$$\left. \frac{\partial \mathcal{L}}{\partial p} \right|_{q \text{ fixed}} = 2\sqrt{q} \cos p + 2q \overbrace{(\cos^2 p - \sin^2 p)}^{2\cos^2 p - 1}$$

$$\begin{aligned} & (e^Q - 1) + 4(e^Q - 1)^2 - 2(e^Q - 1)^2 + \frac{2p^2}{4e^{2Q}} \\ & = 2e^{2Q} - 2e^Q + \frac{p^2}{4e^{2Q}} \end{aligned}$$

$$= \left. \frac{\partial q}{\partial Q} \right|_{p \text{ fixed}}$$